Power Loss Minimization For 11kv Radial Distribution System for Improved Power Quality

CLARKE, A.Y.¹, IDONIBOYEOBU, D.C.², BRAIDE, S. L³

^{1, 2, 3} Department of Electrical Engineering, Rivers State University, Port Harcourt, Nigeria.

Abstract- The distribution system can be seen as the networking line that interfaces between the large power generators and transmission lines on one hand and the electricity consumers on the other. The system can exist in different topologies among which, the radial form is popular because of its simplicity and comparative low cost of design. The problem of poor power quality and instability has been a major power system challenge especially in Nigeria. More reliable and stable power systems among other benefits can be enjoyed when system is optimized. In this research, active and reactive technical power loss was minimized by reactive power injection through placement of capacitor banks. The extent of power loss minimization was considered at different instances based on the absence and presence of capacitors at load buses. The fundamental capacitor sizing equation was deployed and result showed a minimum and maximum reactive power demand of 2100 and 28800 kVAr from 7 and 96 banks respectively. Upon application of adequate capacitor banks power loss minimization was achieved and valued $169 \, kW +$ between j3385 kVAr and 108 kW + j2165 kVAr against a default loss value of 180kW + j3593 kVAr. Obviously, from the results obtained before and after capacitor placement shows achievement of the proposed aim.

Indexed Terms- Power, Minimization, Radial Distribution, system design, modelling

I. INTRODUCTION

Electricity is an essential requirement for all areas of human endeavor. It has almost now been accepted as a basic human need and has been asserted to have the socio- economic development of any country depending on it. Electric power has become a fundamental part of the infrastructure of contemporary society, with most of today's daily activity based on the assumption that the desired electric power is readily available.

The power systems which provide this electricity are some of the largest and most complex systems in the world. They consist of three primary components: the generation system, the transmission system, and the distribution system. Each component is essential to the process of delivering power from the site where it is generated to the customer who uses it. There exist connecting joints in the system, which are known generically as the transmission lines and the distribution networks. Both the transmission and distribution system have prime task of delivering electrical power to customers at their place of consumption and in usable form. While performing this main task, the electric utility is interested in achieving certain sufficient levels of reliability, efficiency, peak load and costs (Kothari, 2013). The subject of distribution loss minimization has gained a great deal of attention due to high cost of electrical energy. This isso because, distribution systems can acquire longer life span and have greater reliability by reducing power losses unit (Kothari, 2013).

The focus of this report is on the application of a suitable solution of the power flow problem for the determination of technical losses and the feeder reconfiguration – an optimization technique for *distribution* systems which aims at minimizing technical losses already determined in the system. Typically, every distribution system originates at a substation where the electric power is converted from the high voltage transmission system to a lower voltage fordelivery to the customers. This work aims at implementing an optimization procedure using feeder reconfiguration for minimizing technical losses on the Rumuola Road 11kV power distribution feeder.

II. LITERATURE REVIEW

• Losses in Power Systems

Losses are inevitable in the provision of electrical energy; even technologically advanced countries cannot make all the electricity generated available for consumer use; some of it is lost just due to the natureof the business of generating, transmitting and distributing electricity.

Electric energy losses are broadly divided into two - technical and non-technical losses.

i. Technical Losses

Technical losses occur because the electrical equipment used in the power system, by nature, have losses associated with them which cannot be totally eliminated. Generators/transformers have losses in their windings (due to the winding resistance) as well as their core (due to eddy current and hysteresis).

ii. Non-Technical Losses

Non-technical losses (also called commercial losses) occur due to energy theft, poorly estimated billing, defective metering equipment (either deliberately tampered with or not), unpaid bills etc. They are generally caused by actions external to the power system and cannot be empirically computed like the technical losses. Energy theft can be done by tampering with meters to make them undercount, bypassing the meters, making illegal connections, colluding with utility company meter readers to falsify consumption data or billing department to alter the bill issued to the customer (Awosope, 2014)

Unbalanced Loads

It is not uncommon to see all the four supply conductors (three phases and neutral) from the secondary distribution transformer connected to the single-phase consumer with wire connections to enable phase selection. Whenever there is loss of supply or excessively low voltage on one phase, consumers would then operate their fuse cut-out to transfer to any phase that is still energized. The realization that supply is still available on other phases usually occurs by observation of nearby houses or through indicators (usually light bulbs) installed at the premises (this in itself constitutes a waste of energy when it is left lit perpetually)

• Lack of Legislation on Electric Energy Theft

Electric energy theft is the illegal use of electricity with the objective of evading tariff payment. In Nigeriait is reported to be committed more by the wealthy and affluent with supposedly high social status (Okafor, 2019). Illegal use occurs when: consumption is done without an agreement, the metering equipment is circumvented, or the meter is interfered with to alter the readings; the main objective being to save money (Okafor, 2019). However, while the energy thieves are saving money, the utility company and even the honest customers are losing money. For example, the Port Harcourt Electricity Distribution company reported a monthly revenue loss of N233 million. Theft is made rather easy because of the physical access of the end users to the electricity infrastructure. Penaltiesimposed in other climes, e.g. in India where fines and imprisonment of up to five years is specified (Okafor, 2019), havenot completely eradicated energy theft. It is worse in Nigeria because there is no law on electrical energy theft (although disconnection and payment of a fee before reconnection is practiced). However, a bill seeking to criminalize and punish electricity theft with fines and jail terms has been submitted to the NationalAssembly by NERC (Smith, 2014).

The review of related literature suggest that a number of studies has been carried out to improve the energy distribution output for a given electrical energy and the losses which appear across the feeder will be used in eliminating or reducing the losses on the system for a maximum efficiency of its output.

Distribution System is an important system in power system. Distribution System can be seen as the networking line that interfaces between the large power generators and transmission lines on one hand and the electricity consumers on the other hand. Electricity utility is interested in achieving certain sufficient levels of reliability, efficiency, peak load and costs but sometimes the reverse becomes the case due to power loss. In developed countries, it is not greater than 10%. However, in developing countries, thepercentage of active power losses is around 20%; therefore, utilities in the electric sector are currently interested inreducing it in order to be more competitive, since theelectricity prices in deregulated markets are related to the system losses, technical and non-technical losses are accounted as 23% of the total input energy. To manage a loss reduction program in a distribution system it is necessary to use effective and efficient computational tools that allow quantifying the loss in each different network element for system losses reduction. In order to increase the efficiency of the distribution electrical networks, a reconfiguration process was applied to improve the reliability indices. The main aim of this research work is to Minimized Power Loss on 11kv Radial Distribution System for Improving the Power Quality. Specifically, the study sought to:

- i. Study and analyze existing systems,
- ii. Collect network data for system design and modelling,
- Ascertain the present state of the system by subjecting it to load flow studies,
- iv. Adopt a good power loss minimization approach for optimal loss reduction, and
- v. Analyze and ensure that the adopted solution after implementation meets the aim of the project by improving the reliability and the efficiency of Rumuola distribution network.

III. MATERIALS AND METHODS

3.1 Simulation Data and Software

The data for simulation was collected from the PHEDC office rumuola branch comprising of 3 months data, June, July and August, from the data's available for the month with the highest peak load was selected to be used as load on that selected 11kV bus. And the Power system simulation software to be used is ETAP (Electrical transient analysis program) while excel is used for data visualization

3.2 Methods

Two methods of solution are deployed in this research; first a load flow is conducted to ascertain the steady state and transient behaviour of the system while a second method for capacitor placement will also be used to calculate reactive power demand as well as amount of capacitor bank needed based on the calculated values. Newton Raphson (NR) nonlinear approach will be used to solve the load flow power equations for appropriate values of real and reactive power flows and losses as well as voltage magnitude and angle. Based on the proceeds of the load flow calculations, further calculations will be made using the capacitor bank placement equation. Equation 3.1 is the fundamental equation for capacitor kVAr sizing for improved power supply through power factor and reactive power improvement.

 $kVAr = kW (tan \phi_1 - tan \phi_2)$

(3.3)

Where $Cos \phi = Power factor (pf)$

$$\phi = Cos^{-1}(pf) \tag{3.2}$$

From equation 3.3 values of ϕ_1 and ϕ_2 known as existing and expected angular values of the power factor will be deduced.

From equation (3.1), KVAr = Capacitor rating value (minimum and maximum)

KW = Average and maximum active power Careful application of the above equations will reveal the effect of capacitor bank placement in the Rumuola distribution network be it positive or negative.

Total factor = 35.8MW $\equiv 35800$ KW

@ Minimum, power will used into average to form numbers of branches

 \therefore average power $\equiv \frac{Total \ power}{2} = \frac{35800}{2} = 17900 KW$

For minimum placement

Given that,

 $\cos \theta_1 = 0.76, \cos \theta_2 = 0.8, KW = 17900$

 $\therefore \theta_{1} = \cos^{-1}(0.76) = 40.54, \theta_{2} = \cos^{-1}(0.8) = 36.87$

Using capacitor bank sizing equation

 $KVAR = KW [\tan \theta_1 - \tan \theta_2]$

KVAR = 17900 [tan 40.54 - tan 36.87]

KVAR = 17900 [0.86 - 0.75]

 $KVAR = 17900 \ge 0.11$

KVAR = 1969

= 1969KVAR

How many 300KVAR banks required will be $\frac{1969}{300} = 6.56 \approx 7$ i.e., 7 x 300KVAR banks of capacitor required for minimum banks For maximum capacitor bank, The desired power factor is taken as 99.9%

Given that,

 $\cos \theta_1 = 0.76, \cos \theta_2 = 0.999, KW = 35800$

 $\therefore \theta_{1=} \cos^{-1}(0.76) = 40.54,$

Again $\theta_{2=}\cos^{-1}(0.999) = 2.56$

Using capacitor bank sizing equation

 $KVAR = KW [\tan \theta_1 - \tan \theta_2]$

KVAR = 35800 [0.81] KVAR = 28998 \therefore total number of 300KVAR banks will be $\frac{28998}{300} =$ 96.06

i.e., 96 x 300KVAR capacitor bank is required for maximum bank

IV. RESULTS

This section discusses the results obtained during the research work and the respective load behaviour in some specific areas as mentioned in the case study.

• Load Flow Network Bus Performance without System Modification



Figure 4.1: Pre-Capacitor Placement Load Flow Result

From the pictorial result displayed in Figure 4.1, out of ten bus bars, four namely buses 3, 4, 5 and 6 are critically overloaded while buses 2, 7, 8 and 9 are marginally overloaded with resultant effect of voltage drop beyond and within the IEEE prescribed limit of $\pm 5\%$. Detailed results as regards power loss minimization will be discussed based on the graphical results in the later figures.



Figure 4.2: Pre-Modification Result for kV and % Voltage Magnitude

The above result from the chart in Figure 4.2 shows the difference between the nominal voltage magnitude and the existing voltage magnitude in terms of kV and % due to system voltage drop. Aside Feeder 3 and Refinery bus maintaining a voltage profile equal to the nominal voltage there is voltage sag in the remaining bus. Power factor, loading and voltage drops as well as real and reactive power flow results along the branches are displayed in Figures 4.3, 4.4 and 4.5.



Figure 4.3: Percentage Pre-Modification Results for Branch Elements

From the results in Figure 4.3, transformers 1 and 2 had the highest loading and voltage drop as 84.6 and 5.62 in terms of percentage but has the least power factor as 75.92%.



Figure 4.4: Pre-Modification Result of Branch Elements against Losses

Both real and reactive power loss results were produced from the pre-modification simulation based on the drops associated with the branch elements. From Figure 4.4, the least joint active and reactive power losses is valued at 36.16 *kW* and 723.1 *kVAr* due to transformer impedances.



Figure 4.5: Pre-Modification Result for Feeder Power Flow

Active and reactive power flow results are displayed in figure 4.5, with the least and highest real and reactive power flow occurring at New GRA and Rumuokwuta feeders with numerical values of 1964.2 kW + j1473.1 kVAr and 5673.2 kW + j4254.9 kVAr respectively. From the premodification results so far. total of а 180kW and 3593kVAr are accounted for as real and reactive power losses awaiting minimization.

4.2 Minimum Modified Results

From the pre-modification result, with an average power of 17631kW, existing branch power factor of 76% and a desired power factor of 80%, the minimum reactive power demand calculated using equation 3.1 is 1939.41*kVAr*. If a capacitor of 300kVAr is to be used, then a minimum of $7 \times 300kVAr$ is being used to supply the total kVAr demand.

The effect of the capacitors placed at bus 5 as it improved the voltage profile of the four critically loaded buses to a marginal point with a minimal power loss reduction from 180kW + j3593kVAr to 169kW + j3385kVAr. Pictorial results showing system improvement through power loss reduction upon $7 \times 300kVAr$ capacitor placement at bus 5 is contained in figure 4.6.





Aside the loss reduction, percentage voltage profile was also increased from 94.38% to 95.07% at buses 3, 4, 5 and 6.



Figure 4.7: Post Modification Result for kV and % Voltage Magnitude with Minimum Banks

Figure 4.7 clearly shows that the voltage variation between the nominal and % voltage magnitude is slim and all buses operating within the prescribed voltage regulation with the least being at the marginal loadable region.



Figure 4.8: Percentage Post Modification Results for Branch Elements with Minimum Banks

© JAN 2022 | IRE Journals | Volume 5 Issue 7 | ISSN: 2456-8880

Upon successful application of minimum capacitor banks, the percentage power factor, loading and voltage drop received appreciable boosting. The minimum and maximum percentage voltage drops was jointly recorded at transformers 3, 4 and 1, 2 as 4.58% and 4.93%. Evidently, the % voltage drop results obtained after minimum bank application showed compliance with the IEEE prescribed limit and a reduction as compared to the highest pre-modification drop result of 5.62%.





Both real and reactive power loss results were produced from the post modification simulation based on the drops associated with the branch elements. From figure 4.9, the least joint active and reactive power losses is valued at 36.16 *kW* and 723.1 *kVAr* due to transformer impedances.

Though the least values were similarly to the premodification values, the maximum loss value experienced a drop from

56.66kW and 1073.3kVAr to 48.46kW and 969.2kVAr



Figure 4.10: Post Modification Result for Feeder Power Flow with Minimum Banks

Active and reactive power flow results are displayed in figure 4.10, with the least and highest real and reactive power flow occurring at New GRA and Rumuokwuta feeders with numerical values of 1964.2 kW + j1473.1 kVAr and 5688.4 kW + j4266.3 kVAr respectively. This huge power flow increase was as a result of the presence of CAP 1 at bus 5 with injection capacity of 1897.9kVAr.

The net power loss as per comparing the pre and post modification results in the absence and presence of minimum capacitor banks resulted in a 7% power loss reduction.

4.3 Maximum Modification Results

From the pre-modification result, with a total power of 35261kW, existing branch power factor of 76% and a desired power factor of 99.9%, the maximum reactive power demand calculated using equation 3.1 is 28746.37kVAr. If a capacitor of 300kVAr is to be used, then a maximum of $96 \times 300kVAr$ is being used to supply the total kVAr demand.



Figure 4.11: Post Capacitor Placement Load Flow Result with Maximum Banks



Figure 4.12: Post Modification Result for kV and % Voltage Magnitude with Maximum Banks

Figure 4.12 clearly shows that the voltage variation between the nominal and % voltage magnitude is negligible and all buses are operating within the prescribed voltage regulation without violation. Judging from the voltage profiles, there is a transition from marginal overloading to a point of best operation.



Figure 4.13: Percentage Post Modification Results for Branch Elements with Maximum Banks

Upon successful application of maximum capacitor banks, the percentage power factor, loading and voltage drop received huge boosting. The minimum and maximum percentage voltage drops was jointly recorded at transformers 3, 4 and 1, 2 as 0.04% and 0.37% which is less than unity. Evidently, the % voltage drop results obtained after minimum bank application showed compliance with the IEEE prescribed limit and a reduction as compared to the highest pre-modification and minimum post modification drop results. Comparatively, results from application of maximum number of capacitor banks 95.98% and 95.69% voltage showed drop optimization between the pre-modification and minimum post modification results. Also, optimal

leading and lagging power factor was achieved with minimum percentage loading across all branch elements. From the results in figure 4.13, jointly the power factor of all branch elements is averagely 99.9%.





Both real and reactive power loss results were produced from the maximum post modification simulation based on the drops associated with the branch elements. From figure 4.14, the least and maximum joint active and reactive power losses is valued as 21.99 kW + j439.7 kVAr and 32.14 kW + j642.8 kVAr due to transformer impedances.

When compared to the pre-modification and minimum post modification simulation results, a loss reduction in the tune of 60 and 64% active power loss minimization.



Figure 4.15: Post Modification Result for Feeder Power Flow

Active and reactive power flow results are displayed in figure 4.15, with the least and highest real and reactive power flow occurring at New GRA and Rumuokwuta feeders with numerical values of 2000.3 kW + j1500.2 kVAr and 5791.4 kW + j4343.5 kVAr respectively. This huge power flow increase was as a result of the presence of CAP 1 and 2 at buses 5 and 8 with operating leading capacity of 28696kVAr.

CONCLUSION

In this study, power loss reduction was successfully conducted in conformity with IEEE voltage regulation standard through voltage profile improvement by means of reactive power injection. Post simulation results clearly fulfils the aim of this research as optimal power loss minimization was achieved using maximum capacitor bank allocation as compared to the pre and post with minimal capacitor placement results. Apparently, results obtained after simulation proved positive as both aim and objectives of the research were fulfilled with violation of standards.

RECOMMENDATIONS

After considering effects of active power losses in distribution system on any nation's economy and cost of electricity, it is recommended that such feeder reconfiguration, capacitor placement among the many optimization techniques be performed on the system. Following the trends in power system technologies worldwide and recent research and development of smart grid technologies, it can be inferred that

- i. Hardware application of the optimization technique implemented in this project
- ii. A comparative review should be carried between the implemented method and introduction of relief transformers
- iii. Smart grid technology should be adopted for lasting power systems solution

REFERENCES

 Amaresh, K. Sivanagaraju, S. & Sankar, V. (2006). Minimization of Losses in Radial Distribution System by using HVDS IEEE Power Electronics, Drives and Energy Systems, 2006. PEDES '06, International Conference,1 – 5

- [2] Anne-Marie, B. & Jan, F. K. (2001). Distributed Generation The Power Paradigm for the New Millennium. CRC Press, Boca Raton London New York Washington, D.C.
- [3] Augugliaro, A. Dusonchet, L. Favuzza, S. & Sanseverino, E.R. (2004). Voltage Regulation and Power Losses Minimization in Automated Distribution Networks by an Evolutionary Multiobjective Approach. *IEEE Transactions* on Power Systems, 19(3).
- [4] Augugliaro, A. Dusonchet, L. Favuzza, S. Sanseverino, E.R. (2004). Voltage Regulation and Power Losses Minimization in Automated Distribution Networks by an Evolutionary Multiobjective Approach. *IEEE Transactions* on Power Systems, (3), 1516 – 1527.
- [5] Berly, J. (1880). <u>Notes on the Jablochkoff</u> <u>System of Electric Lighting</u>. Journal of the Society of Telegraph Engineers. Institution of Electrical Engineers. **IX** (32): 143. Retrieved 2009-01-07.
- [6] Borges, C.L.T & Falcao, D.M. (2003). Impact of Distributed Generation Allocation and Sizing on Reliability, Losses, and Voltage Profile. 2003 IEEE Bologna Power Tech Conference Proceedings, Bologna, 2, 23-26.
- [7] Broadwater, R.P. Khan, A.H. Shaalan, H.E. & Lee, R.E. (2013). Time varying load analysis to reduce distribution losses through reconfiguration. *IEEE Trans. Power Del.*, 8, (1), 294–300.
- [8] Davidson, I.E. & Ijumba, N.M. (2002). Optimization Model for Loss Minimization in a Deregulated Power Distribution Network. 6th IEEE Africon Conference in Africa (AFRICON), Africa, 2-4 Oct. 2002, Vol.2, pp.887 – 894.
- [9] Griffin, T. Tomsovic, K. Secrest, D. & Law, A. (2000). Placement of Dispersed Generations for Reduced Losses. Proceedings of the 33rd Annual Hawaii International Conference on System Sciences.
- [10] Kashem, M.A. Negnevitsky, D.T.M. & Ledwich, G. (2006). Distributed Generation for Minimization of Power Losses in Distribution Systems. *IEEE Power Engineering Society General Meeting*, 8-14.

- [11] Khalil, T.M. Omar, G. M. Sallam, A.A. (2007). Power Losses Minimization and Voltage Profile Enhancement for Distribution Feeders using PSO. IEEE Power Engineering, 2007 Large Engineering Systems Conference, 101 105
- [12] Kothari, D. & Nagrath, I. (2013). Modern Power System Analysis, 4th ed., New Delhi, Tata McGraw Hill Education Private Limited.
- [13] Lin, W. Sheng, Y. Chien, S. Tsay, M. Chen, S. (2000). The Optimal Loss Reduction of Distribution Feeder Based on Special Distribution Transformers Reconnect ion Using Genetic Algorithm. Power System Technology, 2000. Proceedings. *IEEE PowerCon*, *3*, 1413 1418.
- [14] Mehta, V. & Mehta, R. (2014). Principles of Power Systems, New Delhi: S. Chand Publishing.
- [15] Merlin, & Back, H. (2010). Search for a Minimal-Loss Operating Spanning Tree Configuration in Urban Power Distribution Systems. Proc. of 5th Power Systems Comp. Con., Cambridge, U. K.
- [16] Morton, B. & Mareels, I. M. (2000). An efficient brute-force solution to the network reconfiguration problem. *IEEE Trans. Power Syst.*, 15, (3), 996–1000.
- [17] Mutale, J. Strbac, G. Curcic, S. & Jenkins, N. (2000). Allocation of Losses in Distribution Systems with Embedded Generation. *IEE Proceedings of Generation, Transmission and Distribution, 147*(1), pp. 7 14.
- [18] Nigerian Electricity Regulation Commission (NERC), Industry statistics [Online]. Available: https://nercng.org/index.php/library/industrystatistics/distribution/119-
- [19] Ogundipe, A.A. Akinyemi, O. Ogundipe, O.M. (2016). Electricity consumption and economic development in Nigeria, *International Journal of Energy Economics andPolicy*, 6(1), 134-143.
- [20] Peponis, G. J. Papadopoulos, M. P. & Hatziargyriou, N. D. (2012). Optimal operation of distribution networks. *IEEE Trans. Power Syst.*, 11(1), 59–67.

- [21] Quentin, R.S. (2012). The 100 Most Significant Events in American Business: An Encyclopedia, ABC-CLIO, 86
- [22] Ramesh, L. Chowdhury, S.P. Chowdhury, S. Natarajan, A.A. (2008). Voltage Stability Analysis and Real Power Loss Reduction in Distributed Distribution System. IEEE Transmission and Distribution Conference and Exposition, 2008. T&D. IEEE/PES, 1–6.
- [23] Ramesh, L. Chowdhury, S.P. Chowdhury, S. Natarajan, A.A. (2008). Distribution Feeder Restructuring for Better Voltage Regulation and Line Loss Reduction" IEEE Powercon.
- [24] Ramesh, L. Ravindran, S. Chowdhury, S.P. Chowdhury, S. (2007). Distribution System Loss Minimization and Planning using Cymdist" IEEE Universities Power Engineering Conference, 2007. UPEC 2007. 42nd International Conference, 316 321
- [25] Salman, S.K. (2006). The Impact of Embedded Generation on Voltage Regulation and Losses of Distribution Networks. IEE Colloquium onthe Impact of Embedded Generation on Distribution Networks (Digest No. 1996/194), pp. 2/1 – 2/5.
- [26] Schmidt, H. P. Ida, N. Kagan, N. & Guaraldo, J. C. (2005). Fast reconfiguration of distribution systems considering loss minimization. *IEEE Trans. Power Syst.*, 20, (3), 1311–1319.
- [27] Shirmohammadi, D. & Hong, H. W. (2011). Reconfiguration of electric distribution networks for resistive losses reduction. *IEEE Trans. PowerDelivery*, *4*, 1402–1498.
- [28] Short, T.A. (2014). Electric Power Distribution Handbook. Boca Raton, Florida, USA: CRC Press. 1–33.
- [29] Siti, M.W. Nicolae, D.V. Jimoh, A.A. & Ukil, A. (2007). Reconfiguration and Load Balancing in the LV and MV Distribution Networks for Optimal Performance. *IEEE Trans. On Power Delivery*, 22, (4).
- [30] Tsai, M.S. Hsu, F.Y. (2004). Comparison of Genetic Algorithm Reproduction Methods for Distribution System Loss Minimization" Proceedings of the Third IEEE International

Conference on' Machine Learning and Cybemetics, Shanghai.

- [31] Viswanadha, R. G. K. & Bijwe, P. R. (2008). An Efficient Algorithm for Minimum Loss Reconfiguration of Distribution System Based on Sensitivity and Heuristics. *IEEE Trans. On Power Systems*, 23(3).
- [32] Zhang, X. P. (2008). Energy Loss Minimization of Electricity Networks with Large Wind Generation using FACTS. IEEE Power and Energy Society General Meeting. *Conversion and Delivery of Electrical Energy in the 21st Century*, 1-5.