Differential Evolution Based PID Antenna Position Control System

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Abstract- This paper presents a robust and efficient way of tuning PID controller using different variants of differential evolution (DE) algorithms for antenna positioning system. 20 DE variants were implemented out of which DE/rand/1/bin appear to be more promising in addressing this problem with peak overshot of 0.0052, rise time of 0.01sec, and settling time of 0.01sec. This has an overall cost or objective fitness function of 0.0162. The second best optimizer is DE/best/1/exp.

Indexed Terms- Differential evolution algorithms, PID controller, Step response, Ziegler–Nichols tuning method, optimization, objective fitness function.

I. INTRODUCTION

One of the major challenge of any positioning control system is the ability to coup with unpredictable changes resulting from within the system or its environment. Antenna positioning system are face with different challenges among which is disturbance from natural events such as wind. The aim of this research is to design an intelligent control schemes to position the antenna in the direction of the main lobe for optimum reception/transmission in a dynamically changing environment.

II. OPTIMIZATION OR TUNING ALGORITHMS

A brief description of the optimization algorithms implemented are presented in this section. We explore the advantages of global search capability of population based differential evolutionary algorithms variants to evolve the gains of the PID controller. The complexity of many heuristic controllers becomes increasingly complicated due to meta parameters (free parameters) in the model or controller frame work that govern their behaviour and efficiency in optimizing a given problem. How best a given controller can solve a given problem, depends on the correct choice of the meta parameters. The values of those parameters are problem dependent, thus for each problem, those parameters need to be fined tune to get the optimum or near optimum. The tuning pose another optimization problem. The PID gains of the antenna positioning system depicted in this paper were optimized using population based randomization optimization algorithms.

III. DIFFERENTIAL EVOLUTION (DE)

DE are population based direct search algorithms used to solve continuous optimization problems. DE aims at evolving NP population of D dimensional vectors which encodes the G generation candidate solutions $X_{i,G}=X^{1}_{i,G} \dots X^{D}_{i,G}$ towards the global optimum, where $i=1, \dots$ NP. The initial candidate solutions at G=0 are evolves in such a way as to cover the search space as much as possible by uniformly randomizing the candidates within the decision space using Eq (1) [6][7][3].

 $X_{i,G} = X_{min} + rand(1,0). (X_{max} - X_{min})$ (1) Where $i = 1, ..., NP, X_{min} = X_{min}^1 ... X_{min}^D$, $X_{max} = X_{max}^1 ... X_{max}^D$ and rand(1,0) is a uniformly distributed random number between 0 and 1.

3.1 Mutation

For every individuals (target vectors) $X_{i,G}$ at generation G, a mutant vector $V_{i,G}$ called the provisional or trial offspring is generated via certain mutation schemes [6][7][3]. The mutation strategies implemented in this study are:

$$V_{i,G} = X_{r1,G} + F. (X_{r3,G} - X_{r2,G})$$
(2)

DE/best/1:

DE/rand1

$$V_{i,G} = X_{best,G} + F.(X_{r_{2,G}} - X_{r_{1,G}})$$
(3)

DE/rand-to-best/1: $V_{i,G} = X_{i,G} + F.(X_{best,G} - X_{ri,G}) + F.(X_{r2,G} - X_{r1,G})$ (4)

DE/best/2:

$$V_{i,G} = X_{best,G} + F. (X_{r_{2,G}} - X_{r_{1,G}}) + F. (X_{r_{4,G}} - X_{r_{3,G}})$$
(5)

Where the indexes r1, r2, r3 and r4 are mutually exclusive positive integers and distinct from i. These indexes are generated at random within the range [1 - PN]. $X_{best,G}$ is the individual with the best fitness at generation G while F is the mutation constant.

3.2 Cross Over

After the mutants were generated, the offspring U_{i,G} are produced by performing a crossover operation between the target vector X_{i,G} and its corresponding provisional offspring V_{i,G}. The two crossover schemes i.e. exponential and binomial crossover are used in this study for all the DE algorithms implemented. The binomial crossover copied the jth gene of the mutant vector V_{i,G} to the corresponding gene (element) in the offspring $U_{i,G}$ if rand $(0,1) \leq CR$ or $j=j_{rand}$. Otherwise it is copied from the target vector $X_{i,G}$ (parent). The crossover rate CR is the probability of selecting the offspring genes from the mutant while jrand is a random number in the range [1 - D], this ensure that at least one of the offspring gene is copied from the mutant. If CR is small it will result in exploratory moves parallel to a small number of axes of the decision space .i.e. many of the genes of the offspring will come from its parent than from the mutants, consequently the offspring will resemble its parent. In this way, the DE will serve as a local searcher as it bear strong exploitative capabilities than being explorative. On the other hand, large values of CR will lead to moves at angles to the search space's axes as the genes of the offspring are more likely to come from the provisional offspring (mutant vector) than its parent. This will favour explorative moves. The Binomial crossover is represented as:

 $\begin{cases} V_{iG}^{j} \ if \ rand(0,1) \leq CR \ or \ j = j_{rand} \\ X_{iG}^{j} \ Otherwise \end{cases}$ (6)

For exponential crossover, the genes of the offspring are inherited from the mutant vector $V_{i,G} \mbox{ starting from }$

a randomly selected index j in the range [1 - D] until the first time rand(0,1) > CR after which all the other genes are inherited from the parent $X_{i,G}[6][7][3]$.The exponential crossover is as shown in Fig 1.

 $U_{iG} = X_{iG}$ generate = randi(1, D) $U_{iG}^{j} = V_{iG}^{j}$ K = 1 $while rand(0,1) \le CR \text{ and } K < D$ $U_{iG}^{j} = V_{iG}^{j}$ j = j + 1 $if \ j = D \ then$ j = 1 $end \ if$ K = K + 1 $end \ while$

Fig. 1: Exponential crossover

3.3 Selection process

When the offspring U_{iG} is birthed via the crossover scheme, to determine whether the offspring should replace its parent XiG or not in the next generation, a greedy selection schemes based on Darwinian Theory is employed. The cost functions (commonly referred to as the fitness functions) $f(U_{iG})$ and $f(X_{iG})$ of the offspring and its parent respectively are computed and compared. If $f(U_{iG}) < f(X_{iG})$ the offspring will replaced its parent in the next generation i.e. $X_{iG+1} = U_{iG}$ otherwise its parent will be allowed to continue in the next generation $X_{iG+1}=X_{iG}$. This scheme is based on the principles of survival of the fittest. The fitness function used in this research is the weighted sum of the overshot (over or under shot), rise time and the settling time when a unit step input command is used.

3.4 jDE

As is always the case in many optimization problems to be solved using heuristic optimization algorithms, the best optimizer for the particular problem is often not known prior to trial. Hence we deem it fit to try one of the famous variant of DE called jDE. The jDE scheme is a popular way of enhancing DE performance with a very modest programming effort. The jDE algorithm enhance the pool of DE search moves by including a certain degree of randomization into the original DE framework. In <u>jDE</u>, the values of mutation and crossover are encoded within each individual candidate solution. For example, the generic individual X_i will be composed of

$$X_{i} = (X_{i}[1], X_{i}[2], \dots, X_{i}[D], F_{i}, CR_{i})$$
(7)

Hence, at every generation, the offspring is generated for each individual with the parameters F_i and CR_i belonging to its parent. Furthermore, these parameters are periodically refreshed on the basis of the following randomized criterion [6][7]:

$$F_{i} = \begin{cases} F_{L} + F_{U}.rand1 \ if \ rand2 \ < \mathcal{T}_{1} \\ F_{i} \qquad 0 therwise \end{cases}$$
(8)

$$CR_{i} = \begin{cases} rand3 \ if \ rand4 < T_{2} \\ CR_{i} \quad Otherwise \end{cases}$$
(9)

Where rand_j, j=[1,2,3,4] are uniform pseudo-random values between 0 and 1. \mathcal{T}_1 and \mathcal{T}_2 are constant values which represent the probabilities of updating the parameters F_i and CR_i respectively, F_L and F_U are constant values which represent the minimum value that F could take and the maximum variable contribution to F, respectively.

3.5 Fitness Function Evaluation

The optimization problem presented in this paper is a multi-objective optimization problem since there are three cost functions we want to minimise i.e. the maximum overshot (M_o), rise time (T_r) and settling time (T_s). In order to get a robust controller gains, the problem is converted to single objective problem with one cost function consisting of the weighted sum of the three objective functions, Eq (10). The weights depends on the important or cost of risk resulting from that particular performance index. This approach is robust because different models can be evolved by just changing the weight to meet up with setting performance specifications.

$$\gamma = \alpha_o M_o + \alpha_r T_r + \alpha_s T_s \tag{10}$$

Where: γ is the fitness function, M_o is the maximum overshot, T_r is the rise time and T_s settling time, while α_o , α_r , and α_s are their weights respectively. For this research, after a manual tuning, the following values were used with M_o having the highest priority, $\alpha_o=1$, $\alpha_r=0.5$, and $\alpha_s=0.6$. Note the maximum value the weight can take for this application is 1.

IV. PROPORTIONAL PLUS INTEGRAL PLUS DERIVATIVE (PID) CONTROLLER

It is interesting to know that nearly half of the industrial controllers used today are PID or modified PID or derivatives of PID controllers. Some intelligent controllers e.g. Fuzzy logic or adaptive fuzzy logic are derivatives of basic PID i.e. they make use of the error and its derivative (rate of change of the error). There are different variant of the PID controller, the one used in this research is given by equation (11) while the transfer function $G_c(s)$ of the controller is depicted by Eq (12), [2][1][4]. A proportional controller will have the effect of reducing the rise time, but will not eliminate the steady-state error. Because of the present of pole at the origin introduced by the integral controller, the integral control will have the capability of eliminating the steady-state error, but it may make the transient response worse. The derivative control will have the effect of increasing the stability of the system, reducing the overshoot, and improving the transient response. The derivative controller predict future error using the rate at which the error is changing while the integral captured the cumulative effects of past errors to improve the system performance.

$$PID = K_p(e(t) + \frac{1}{T_i} \int_{t_0}^t e(t) dt + T_d \frac{de(t)}{dt})$$
(11)
$$G_c(s) = K_p(1 + \frac{1}{T_i s} + T_d s)$$
(12)

Where: t is time, e(t) is present error at time t, K_p is the proportional gain while T_i and T_d are integral and derivative time constants respectively, s is Laplace complex notation.

4.1 Tuning of the PID gains (K_p , T_i and T_d) Ziegler-Nichols

The process of selecting the controller parameters K_{p} , T_i and T_d to meet a given performance specifications is known as controller tuning. Different variant of population based differential evolution (DE) algorithms were used to evolve the PID gains. One of the major challenge is to define the decision search space i.e. the range within which each of the meta parameters (K_p , T_i and T_d) of the controller should be searched. To address this problem, Ziegler-Nicholstuning method was used to obtain the centre of the radius of the search space. The Ziegler-Nichols reference gains were obtained using the mathematical model of the antenna positioning system shown in Fig. (2). The centre of the radius for each of the gains K_{p} , T_i and T_d are given by equations (13), (14) and (15) respectively [2].

$$K_p = 0.6K_{cr} \tag{13}$$

$$T_i = 0.5P_{cr} \tag{14}$$

$$T_d = 0.125 P_{cr}$$
 (15)

Where K_{cr} and P_{cr} are the critical gain and critical frequency for self-sustained oscillation of the system. The decision search space for each of the gains were obtained as follows:

$$K_{p(space)} = [\alpha_{min}K_p, \ \alpha_{max}K_p]$$
(16)

$$T_{i(space)} = [\beta_{min}T_i, \ \beta_{max}T_i] \tag{17}$$

$$T_{d(space)} = [\mu_{min}T_d, \ \mu_{max}T_d] \tag{18}$$

 K_p , T_i and T_d are given by equations (13), (14) and (15) respectively while after a manual tuning, the minimum and maximum values of α , β and μ were obtained as follows:

$$\alpha_{min} = 0.4, \qquad \beta_{min} = 0.2, \ \mu_{min} = 0.2, \ \alpha_{max} = 5, \qquad \beta_{max} = 4, \ \mu_{max} = 4$$

V. MATHEMATICAL MODEL OF THE ANTENNA POSITIONING SYSTEM

The rotation of the antenna is achieved using DC motor. The aim is to ensure that the antenna (dish) is in line of side with the main lobe for maximum reception.

$$V = R_a I_a + L_a \frac{dI_a}{dt} + E_b \tag{19}$$

$$T = J\frac{dw}{dt} + Fw \tag{20}$$

$$E_b = K_b w \tag{21}$$

$$T = K_t I_a \tag{22}$$

$$w = \frac{d\theta}{dt} \tag{23}$$

Where V is motor terminal supply voltage, R_a armature resistance, L_a is armature inductance, I_a is armature current, E_b is back emf (electromotive force), T is the torque, w is the angular speed in rad/s, J is the inertia constant while F is the viscose constant, K_b is the back emf constant, t is time and Θ is angular position in rad. The block diagram shown in Fig. 2 was obtain using equations (19) to (23) along with the controller, where Θ_R is the command reference input angle while Θ is the actual output.

VI. RESULTS

Each of the DE variant is run for 400 generations consisting of 20 potential candidate solutions. At the end of the generation, the must fitted (best) candidate is used to set the PID gains. The fitness function used during the training is the weighted sum of the maximum overshot, rise time and settling time, Eq. (10). The evolved best candidate was used to control the antenna positioning system using three different approaches, i.e. the system was tested using standard ram and parabolic input command. Thirdly a real world scenario was modelled as a command input to see how the output of the system can track the target input. The performance index used to evaluate the accuracy of the system in tracking the command in put is the root mean square error (RMSE) given by Eq. (24). It is interesting to note that the fact that the system depicted good performance for standard ram and parabolic input with low RMSE does not necessarily mean that the system will perform well when subjected to real world scenario. This is revealed when the untune controller obtain directly using Ziegler-Nichols method was used. The RMSE of ram and parabolic command using untune PID for a given DE variant shown in Fig. 6 and Fig. 5 are 0.0164 and 0.0598 respectively while for the tuned PID are 0.0212 and 0.0042 respectively. But when the tuned and the untune PIDs were tested using real world command input, the untune PID perform poorly with RMSE of 5.7804 while the tuned PID followed the command input closely with RMSE of 1.8479 as shown in Fig. 4. This research also validate that PID gains obtained using Ziegler–Nichols method may not be the optimum but is a useful tool for obtaining the radius of the search space within which the optimum or near optimum are likely to be found. The details of the numeric results obtained from the DE variants implemented in this research are shown in table 1. 20 DE variants were implemented. Where bin refer to Binomial crossover and exp refer to exponential crossover.

$$RMSE = \sqrt{\frac{1}{N} \sum_{i=1}^{N} (\Theta_{Ri} - \Theta_i)^2}$$
(24)

Where: RMSE is the root mean square error, N is the number of simulation time steps, Θ_{Ri} and Θ_i are the command input and the actual output at time index I respectively.

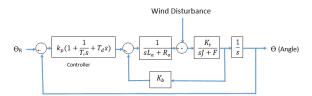


Fig. 2: Block diagram of the antenna positioning system

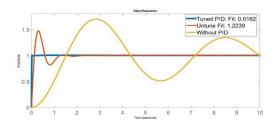
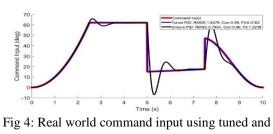


Fig. 3: Unit step response using: tuned PID, untune PID and without PID



untune PID

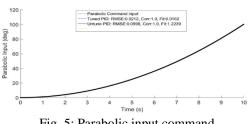


Fig. 5: Parabolic input command

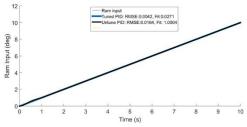


Fig. 6: Ram input command

Table 1: Performance of the various DE variants implemented

Algorithms	RMSE for Three Inputs			Max	Rise	Settling	Fitness
	Real	Ram	Parabolic	Overshot	Time	Time	
	world						
DE/rand/1/bin	1.8479	0.0027	0.0212	0.0052	0.010	0.010	0.0162
DE/rand/1/JDE/bin	2.2223	0.0046	0.0359	0.0122	0.030	0.050	0.0572
DE/rand/1/exp	1.8612	0.0030	0.0231	0.0052	0.010	0.010	0.0162
DE/rand/1/JDE/exp	1.8556	0.0031	0.0236	0,0051	0.010	0.010	0.0161
DE/rand/2/JDE/bin	1.8563	0.0036	0.0286	0.0057	0.010	0.010	0.0167
DE/rand/2/bin	1.8497	0.0029	0.0222	0.0051	0.010	0.010	0.0161

DE/rand/2/JDE/exp	1.8786	0.0034	0.0272	0.0061	0.010	0.010	0.0171
DE/rand/2/exp	1.9040	0.0030	0.0228	0.0063	0.010	0.020	0.0233
DE/best/2/bin	1.8515	0.0031	0.0235	0.0050	0.010	0.010	0.0160
DE/best/2/exp	1.8488	0.0029	0.0222	0.0052	0.010	0.010	0.0162
DE/best/2/JDE/bin	1.8504	0.0030	0.0228	0.0051	0.010	0.010	0.0161
DE/best/2/JDE/exp	1.8490	0.0028	0.0217	0.0052	0.010	0.010	0.162
DE/best/1/bin	1.8500	0.0029	0.0225	0.0051	0.010	0.010	0.0161
DE/best/1/exp	1.8486	0.0028	0.0212	0.0052	0.010	0.010	0.0162
DE/best/1/JDE/bin	1.8564	0.0028	0.0213	0.0054	0.0100	0.010	0.0164
DE/best/1/JDE/exp	1.8505	0.0030	0.0229	0.0051	0.0100	0.010	0.0161
DE/rand/to/best/1/bin	1.8515	0.0030	0.0235	0.0050	0.0100	0.010	0.0160
DE/rand/to/best/1/exp	1.8521	0.0028	0.0216	0.0054	0.0100	0.010	0.0164
DE/rand/to/best/1/JDE/bin	1.8515	0.0031	0.0235	0.0050	0.0100	0.010	0.0160
DErand/to/best/1/JDE/exp	1.9572	0.0038	0.0298	0.0078	0.0100	0.020	0.0248

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CONCLUSION

DE proved to be an efficient optimizer for tuning the PID gains with DE/rand/1/bin algorithm emerging as the best for addressing this particular control problem with RMSE of 1.8479followed by DE/best/1/exp with RMSE 1.8486. It is interesting to note that both algorithms has the same weighted fitness of 0.0162

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